



| DEPARTMENT OF APPLIED MATHEMATICS | | LP: MA16453 |
|-----------------------------------|--|------------------|
| B.E/B.Tech | : Common to CS and IT | Regulation:2016 |
| Sub. Code / Sub. Name | : MA16453 / PROBABILITY AND QUEUING THEORY | Rev. No: 00 |
| Unit I | : Random Variables | Date: 11.12.2017 |

Unit Syllabus: Random Variables

Discrete and continuous random variables - Moments - Moment generating functions , Binomial, Poisson ,Geometric, Uniform, Exponential, Gamma, and Normal distributions.

Objective: To introduce the concept of random variables and deal with various probability distributions.

| Session No. | Topics to be covered | Ref | Teaching Aids |
|--|--|---------------------|---------------|
| 1 | Introduction to unit I. Random variables. | T-1,Ch-2,pg.59-61 | BB/PPT |
| 2 | Probability mass function, probability density function. | T-1,Ch-2,pg.62-75 | BB/PPT |
| 3 | Moments | T-1,Ch-3,pg.85-101 | BB/PPT |
| 4 | MGF and problems based on MGF | T-1,Ch-3,pg.85-101 | BB/PPT |
| 5 | Binomial Distribution. | T-1,Ch-4,pg.111-115 | BB/PPT |
| 6 | Poisson Distribution. | T-1,Ch-4,pg.130-132 | BB/PPT |
| 7 | Geometric Distribution. | T-1,Ch-4,pg.116-120 | BB/PPT |
| 8 | Uniform Distribution. | T-1,Ch-4,pg.141-143 | BB/PPT |
| 9 | Exponential Distribution. | T-1,Ch-4,pg.133-136 | BB/PPT |
| 10 | Gamma Distribution. | R-3,Ch-3,pg.126-128 | BB/PPT |
| 11 | Normal Distribution. | T-1,Ch-4,pg.144-147 | BB/PPT |
| 12 | Summarizing the unit. | T-1,Ch-4,pg.111-153 | BB/PPT |
| Content beyond syllabus covered (if any):Application of One dimensional random variable in real life problem | | | |

* Session duration: 50 minutes



Sub. Code / Sub. Name: MA16453 PROBABILITY AND QUEUEING THEORY

Unit II Two dimensional random variables

Unit syllabus: Two dimensional random variables

Joint Distributions - Marginal and conditional distributions – Covariance - Correlation and Linear regression - Transformation of random variables.

Objective: To introduce the concept of two dimensional random variable, correlation and linear regression.

| Session No | Topics to be covered | Ref | Teaching Aids |
|------------|--|----------------------|---------------|
| 13 | Introduction - Unit Syllabus - Joint distributions. | T-1,Ch-5,pg.167-173 | BB/PPT |
| 14 | Marginal distributions. | T-1,Ch-5,pg.167-173 | BB/PPT |
| 15 | Conditional distributions. | T-1,Ch-5,pg.178-182 | BB/PPT |
| 16 | Problems based on Marginal and Conditional distributions | T-1,Ch-5,pg.173-175 | BB/PPT |
| 17 | CAT I | | |
| 18 | Covariance. | T-1,Ch5,pg.184-186 | BB/PPT |
| 19 | Properties, Problems on Correlation . | T-1,Ch-5,pg.184-186 | BB/PPT |
| 20 | Linear Regression – properties. | T-1,Ch-11,pg.418-422 | BB/PPT |
| 21 | Problems on regression. | T-1,Ch-11,pg.418-422 | BB/PPT |
| 22 | Transformation of random variables | T-1,Ch-6,pg.197-215 | BB/PPT |
| 23 | Problems on Transformation of random variables | T-1,Ch-6,pg.197-215 | BB/PPT |
| 24 | Summarization of Unit-II. | T-1,Ch-5,pg.167-190 | BB/PPT |

Content beyond syllabus covered (if any): Application of Correlation and Regression in real life problem

* Session duration: 50 mins

**Sub. Code / Sub. Name: MA16453 PROBABILITY AND QUEUEING THEORY****Unit III : Random Processes****Unit syllabus: Random Processes**

Classification - Stationary process - Markov process - Poisson process - Discrete parameter Markov chain - Chapman Kolmogorov equation- Limiting distributions-

Objective:

To understand and characterize phenomena which evolve with respect to time in a probabilistic manner.

| Session No | Topics to be covered | Ref | Teaching Aids |
|------------|---|---|---------------|
| 25 | Random processes- Introduction, classification. | T-1,Ch-8,pg.267-273 | BB/PPT |
| 26 | Stationary process – Wide Sense Stationary | T-1,Ch-8,pg.275-282 | BB/PPT |
| 27 | Strict Sense Stationary | T-1,Ch-8,pg.275-282 | BB/PPT |
| 28 | Markov Process | T-1,Ch-10,pg.358-359 R-3,Ch-7,pg.309-316 | BB/PPT |
| 29 | Markov Chain | T-1,Ch-10,pg.359-376 R-3,Ch-7,pg.309-316 | BB/PPT |
| 30 | Problems based on Markov Process. | T-1,Ch-10,pg.359-376 R-3,Ch-7,pg.309-316 | BB/PPT |
| 31 | Transition probabilities | T-1,Ch-10,pg.359-376 R-3,Ch-7,pg.311-317 | BB/PPT |
| 32 | Limiting distributions | T-1,Ch-10,pg.359-376 R-3,Ch-7,pg.317-324 | BB/PPT |
| 33 | Poisson Process - Properties | T-1,Ch-10,pg.342-356 R-3,Ch-6,pg.283-291 | BB/PPT |
| 34 | Poisson Process - Problems | T-1,Ch-10,pg.342-356 R-3,Ch-6,pg.283-291 | BB/PPT |
| 35 | Summarization of unit. | T-1,Ch-10,pg.378 | BB/PPT |
| 36 | CAT II | | |

Content beyond syllabus covered (if any): Application of Random processes in signal processing

* Session duration: 50 mins

**Sub. Code / Sub. Name: MA16453 PROBABILITY AND QUEUEING THEORY****Unit IV : Queuing Models****Unit syllabus: Queuing Models**

Markovian Queues – Birth and Death Processes- Single and multiple server queuing models-Little's Formula - Queues with finite waiting rooms- Finite source models

Objective:

To be exposed to basic characteristic features of a queuing system and acquire skills in analyzing queuing models.

| Session No | Topics to be covered | Ref | Teaching Aids |
|--|--|---------------------|---------------|
| 37 | Queueing system – introduction | T-2,Ch-1,pg.1-7 | BB/PPT |
| 38 | Markovian Models. | T-2,Ch-1,pg.1-45 | BB/PPT |
| 39 | Birth and Death Process. | T-2,Ch-1,pg.1-45 | BB/PPT |
| 40 | M/M/1, Infinite Capacity | T-2,Ch-2,pg.53-68 | BB/PPT |
| 41 | M/M/1, Infinite Capacity | T-2,Ch-2,pg.53-68 | BB/PPT |
| 42 | M/M/1, Finite Capacity | T-2,Ch-2,pg.53-68 | BB/PPT |
| 43 | M/M/1, Finite Capacity | T-2,Ch-2,pg.53-68 | BB/PPT |
| 44 | M/M/c, Infinite Capacity | T-2,Ch-2,pg.69-73 | BB/PPT |
| 45 | M/M/c, Infinite Capacity | T-2,Ch-2,pg.69-73 | BB/PPT |
| 46 | M//M/c, Finite Capacity | T-2,Ch-2,pg.69-73 | BB/PPT |
| 47 | Little's Formula | T-2,Ch-2,pg.53-115 | BB/PPT |
| 48 | Finite source models, Summarization of unit. | T-2,Ch-5,pg.209-260 | BB/PPT |
| Content beyond syllabus covered (if any): Application of queuing models in real life problem | | | |

* Session duration: 50 mins

**Sub. Code / Sub. Name: MA16453 PROBABILITY AND QUEUEING THEORY****Unit V : Non-Markovian Queues And Queue Networks****Unit Syllabus: Non-Markovian Queues And Queue Networks**

M/G/1 queue- Pollaczek- Khintchine formula- M/D/1 and M/EK/1 as a special cases - series queues- Open Jackson Networks.

Objective: Detail study of non-Markovian queues

| Session No. | Topics to be covered | Ref | Teaching Aids |
|--|-----------------------------------|--|---------------|
| 49 | Introduction to unit V | T-2,Ch-5,pg.209-260 | BB/PPT |
| 50 | M/G/1 queue | T-2,Ch-5,pg.209-260 R-3,Ch-7,pg.336-343 | BB/PPT |
| 51 | Pollaczek- Khintchine formula | T-2,Ch-5,pg.211-214 | BB/PPT |
| 52 | Problems on M/G/1 queue | T-2,Ch-5,pg.213-214 R-3,Ch-7,pg.336-343 | BB/PPT |
| 53 | M/D/1 and M/EK/1 as special cases | T-2,Ch-5,pg.209-260 | BB/PPT |
| 54 | M/D/1 and M/EK/1 as special cases | T-2,Ch-5,pg.209-260 | BB/PPT |
| 55 | Series queues | T-2,Ch-4,pg.167-173 R-3,Ch-9,pg.411-415 | BB/PPT |
| 56 | Series queues | T-2,Ch-4,pg.167-173 R-3,Ch-9,pg.411-415 | BB/PPT |
| 57 | Open Jackson Networks | T-2,Ch-4,pg.174-182 R-3,Ch-9,pg.416-422 | BB/PPT |
| 58 | Open Jackson Networks | T-2,Ch-4,pg.174-182 R-3,Ch-9,pg.416-422 | BB/PPT |
| 59 | Summarization of unit. | T-2,Ch-4,5,pg.167-260 | BB/PPT |
| 60 | CAT III | | |
| Content beyond syllabus covered (if any): Application of queuing models in real life problem | | | |

* Session duration: 50 mins

**Sub Code / Sub Name: MA16453 PROBABILITY AND QUEUEING THEORY****TEXT BOOKS:**

1. O.C. Ibe, "Fundamentals of Applied Probability and Random Processes", Elsevier, 1st Indian Reprint, 2007.
2. D. Gross and C.M. Harris, "Fundamentals of Queueing Theory", Wiley Student edition, 2004.

REFERENCES:

1. Robertazzi, "Computer Networks and Systems: Queueing Theory and performance evaluation", Springer, 3rd Edition, 2006.
2. H.A. Taha, "Operations Research", Pearson Education, Asia, 8th edition, 2007.
3. Veerarajan. T, "Probability, statistics and random processes", McGraw Hill Publishers, 3rd edition, 2011.
4. Hwei Hsu, "Schaum's Outline of Theory and Problems of Probability, Random Variables and Random Processes", Tata McGraw Hill Edition, New Delhi, 2004
5. Yates. R.D. and Goodman. D. J., "Probability and Stochastic Processes", Wiley India Pvt. Ltd. Bangalore, 2nd Edition, 2012.

| | Prepared by | Approved by |
|-------------|---------------------|-------------------------|
| Signature | | |
| Name | N.S.Priya | Dr. R. Muthucumaraswamy |
| Designation | Assistant Professor | Professor & Head |
| Date | 11.12.2017 | 11.12.2017 |

* If the same lesson plan is followed in the subsequent semester/year it should be mentioned and signed by the Faculty and the HOD